

Re: My claim on Omega's defn

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|—|erc wrote:

> $\Omega = \sum (p \text{ halts}) 1 / (2^{\text{size}(p)})$

>

> [big snip]

>

> *Even with infinitesimally small total probability of halting, Omega will not converge and will equal oo.*

You seem to be missing the point that the domain of the universal self-delimiting TM U is taken to be prefix-free — ie, the encoding of halting TMs is such that if x is the encoding of some halting TM, then no proper prefix of x is a encoding. Basically, any branch of the infinite-binary tree will contain at most one such encoding, and so to simply say that there are 2^n encoding with n bits is just being ignorant. It follows via Kraft's inequality that Chaitin's Omega will be bounded.

> *Now try the modified Omega.*

>

> *If all programs halt*

>

> $\Omega' = 1/4 + 1/4 + 1/16 + 1/16 + 1/64 + 1/64 + 1/64 + 1/64 + 1/256 + ..$

> $= 1/4 + 1/4 + 1/8 + 1/16 + 1/32...$

> $= 0.75$

>

> *You could disallow the 1st program, 0, so it adds to 1.*

>

>

> $\Omega' = \sum (p \text{ halts}) 2^{-|p|}$

How will your "omega" correspond to the "probability that a program halts"? This seems to be one of the most important aspects of Chaitin's constant, though you just seem to be taking a naive approach to ensure that things will work out.

You do not seem to have invested any time into any sort of worthwhile literature-search. Even a Google search will lead you to various papers by Calude, Chaitin, etc. that will show your objections are founded only

comp.theory: Re: My claim on Omega's defn

on ignorance. Try, perhaps, the first 3 sections of
<http://www.cs.auckland.ac.nz/CDMTCS//researchreports/059cris.pdf>

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Arthur